

# Improvements in Modeling Radiant Emission from the Interaction Between Spacecraft Emanations and the Residual Atmosphere in LEO

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# Outline

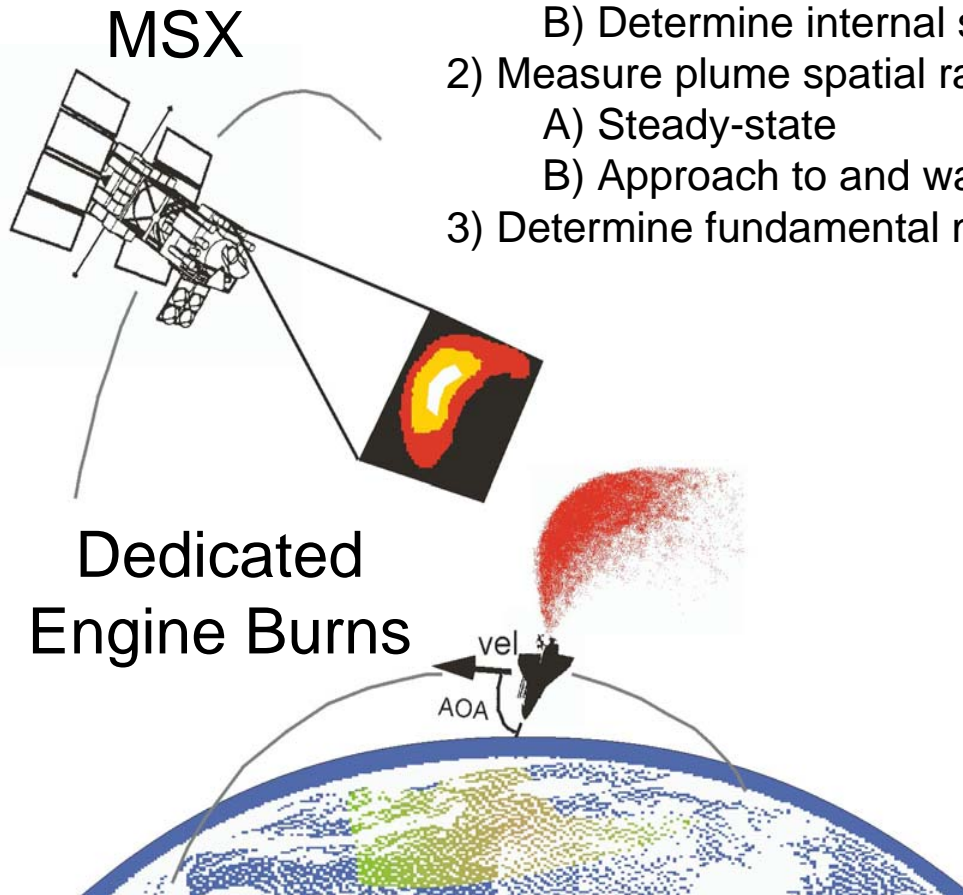
- **Introduction and Background**
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- **Summary & Conclusions**

# Introduction and Background

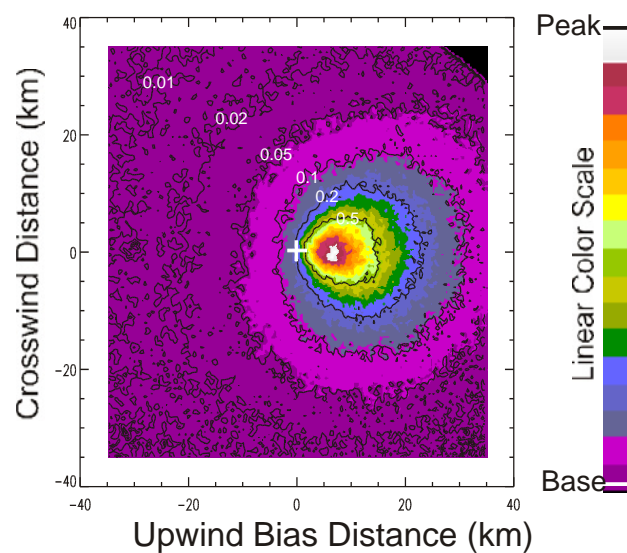
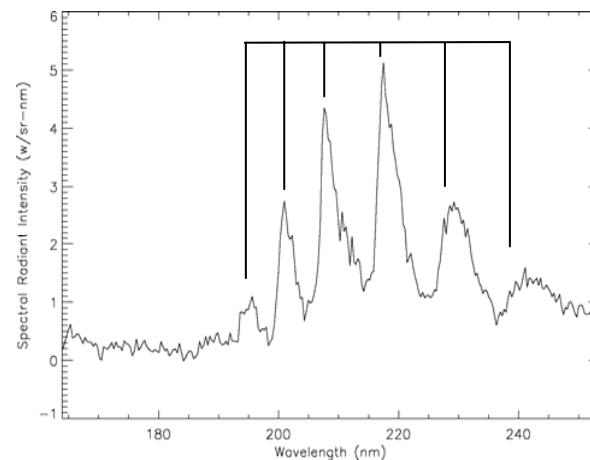
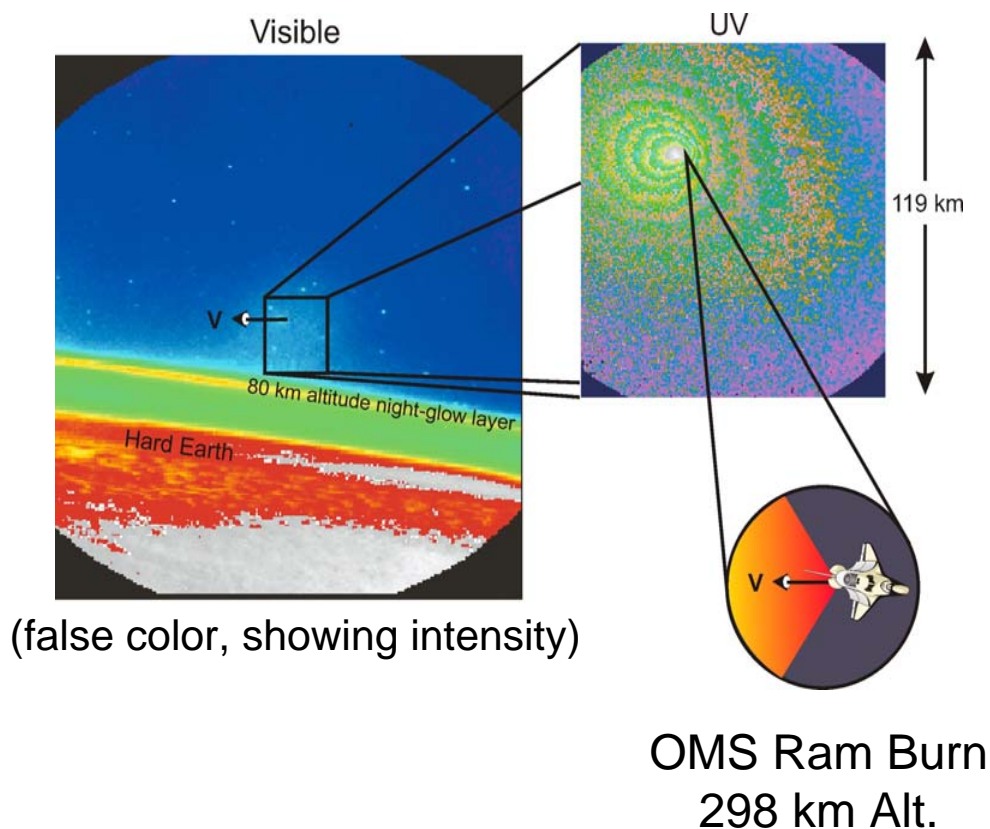
# Data Which Revealed Need

## Shuttle Plume Observations Experiment

- 1) Measure plume spectral radiance
  - A) Identify emitters
  - B) Determine internal state distributions
- 2) Measure plume spatial radiance from emitters
  - A) Steady-state
  - B) Approach to and wane from steady-state
- 3) Determine fundamental mechanisms

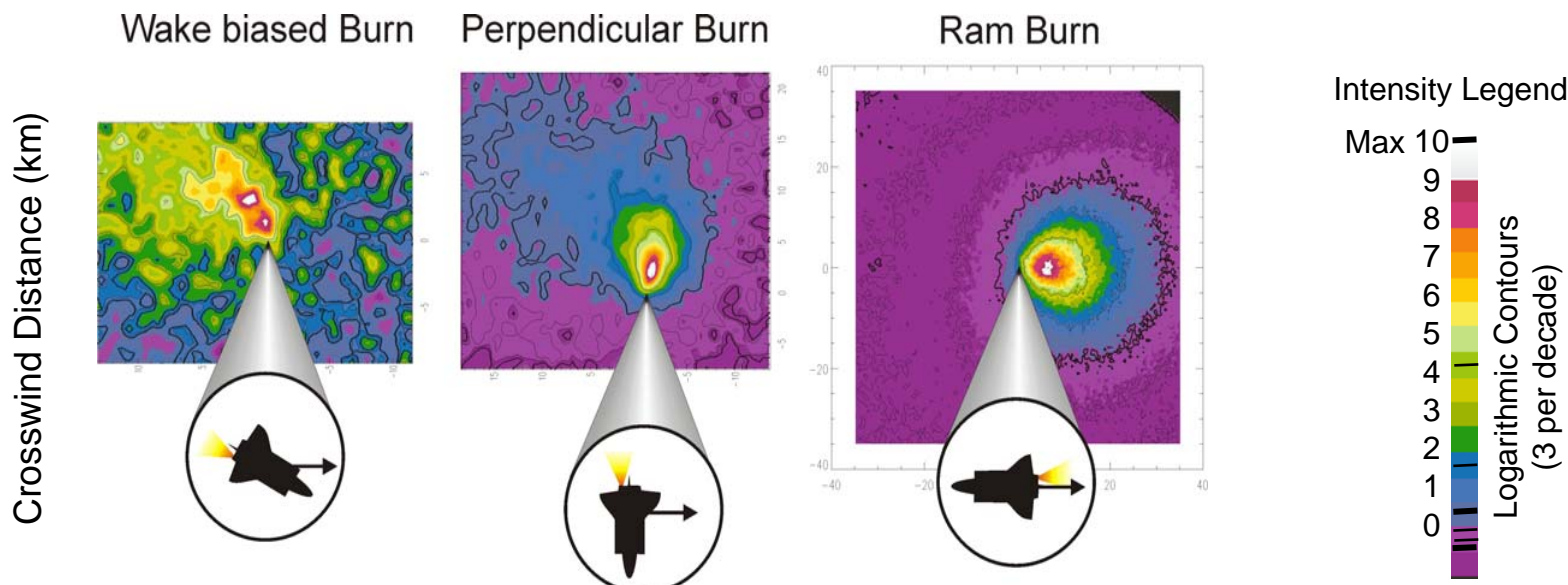


# CO Cameron Band Emission



Total intensity = 1940 W/sr  
~1 photon/10,000 plume molecules

# AOA Dependence



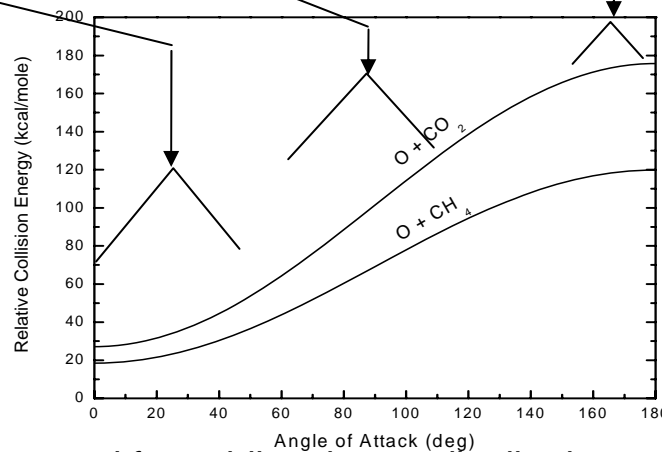
Atm. Density =  $9.9 \times 10^8$   
Peak =  $4.8 \times 10^{-11}$  W/sr-cm<sup>2</sup>  
Total = 31 W/sr

Atm. Density =  $9.2 \times 10^8$   
Peak =  $4.3 \times 10^{-10}$  W/sr-cm<sup>2</sup>  
Total = 414 W/sr

Atm. Density =  $2.8 \times 10^8$   
Peak =  $5.2 \times 10^{-10}$  W/sr-cm<sup>2</sup>  
Total = 2140 W/sr

## Atmosphere Composition

O	0.7 – 0.9
N <sub>2</sub>	0.1 – 0.26
O <sub>2</sub>	0.003 - .01
O <sup>+</sup>	0.0005 - .0001



## Exhaust Composition

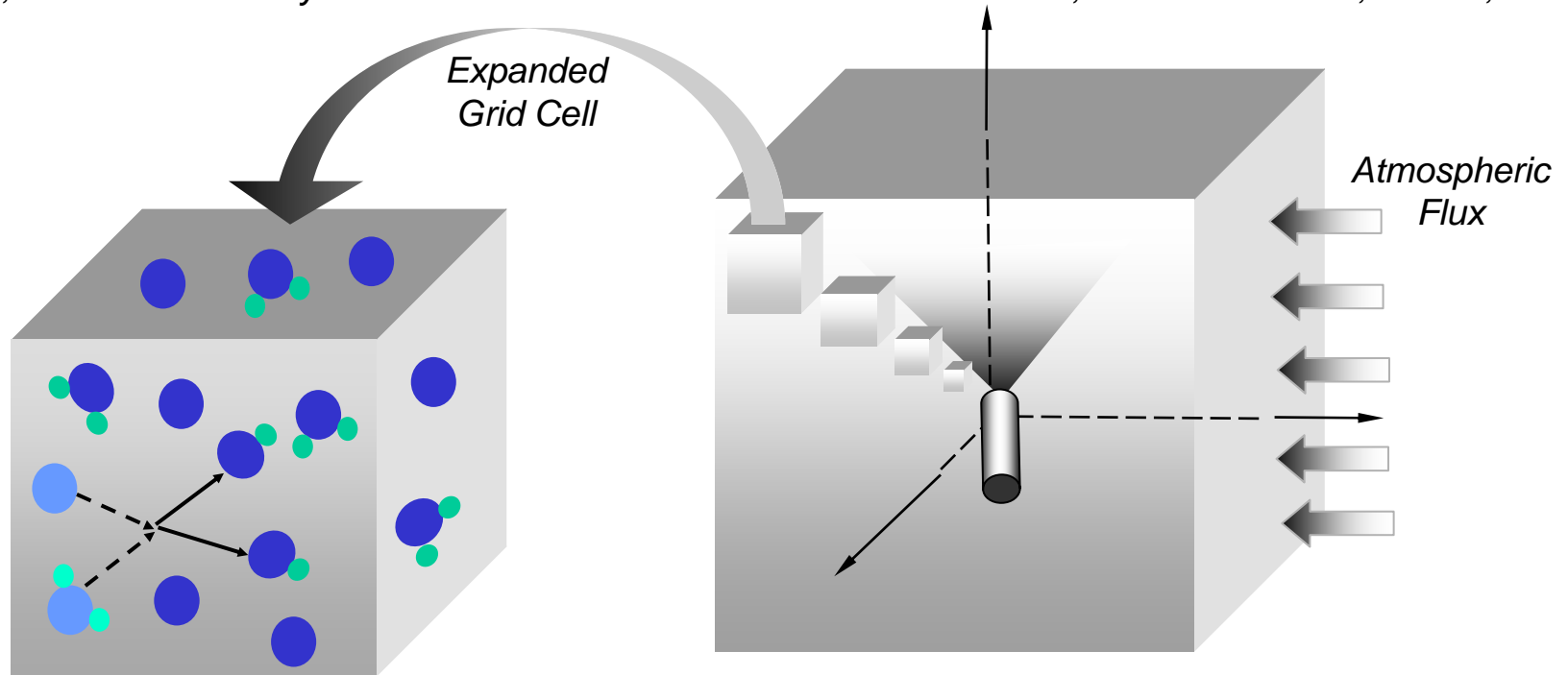
H <sub>2</sub> O	0.32
N <sub>2</sub>	0.31
H <sub>2</sub>	0.17
CO	0.12
CO <sub>2</sub>	0.05
H	0.015



# Plume Modeling

## SOCRATES: Direct Simulation Monte Carlo (DSMC)\*

\*G.A. Bird, "Molecular Gas Dynamics and the Direct Simulation of Gas Flows", Clarendon Press, Oxford, 1994.



### DSMC algorithm

- Advance Molecules
- Simulate Collisions
- Sample Outcomes

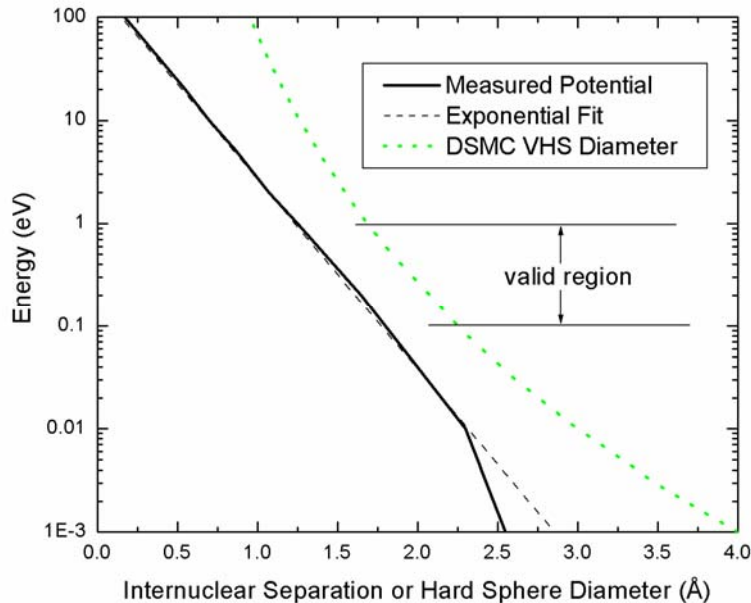
Macroscopic quantities are determined from statistical averages of microscopic events

$\sim 10^6$  "particles"  
 $\sim 10^4$  grid cells

Interactions must be simple to minimize computational burden



# Variable Hard Sphere (VHS) Model



Particle sizes determined from

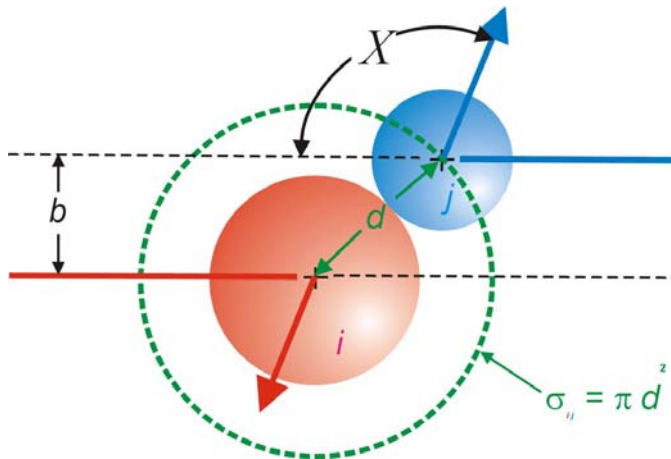
$$E = A / d^n \quad (n = 8) \quad (1)$$

Which conveniently yields

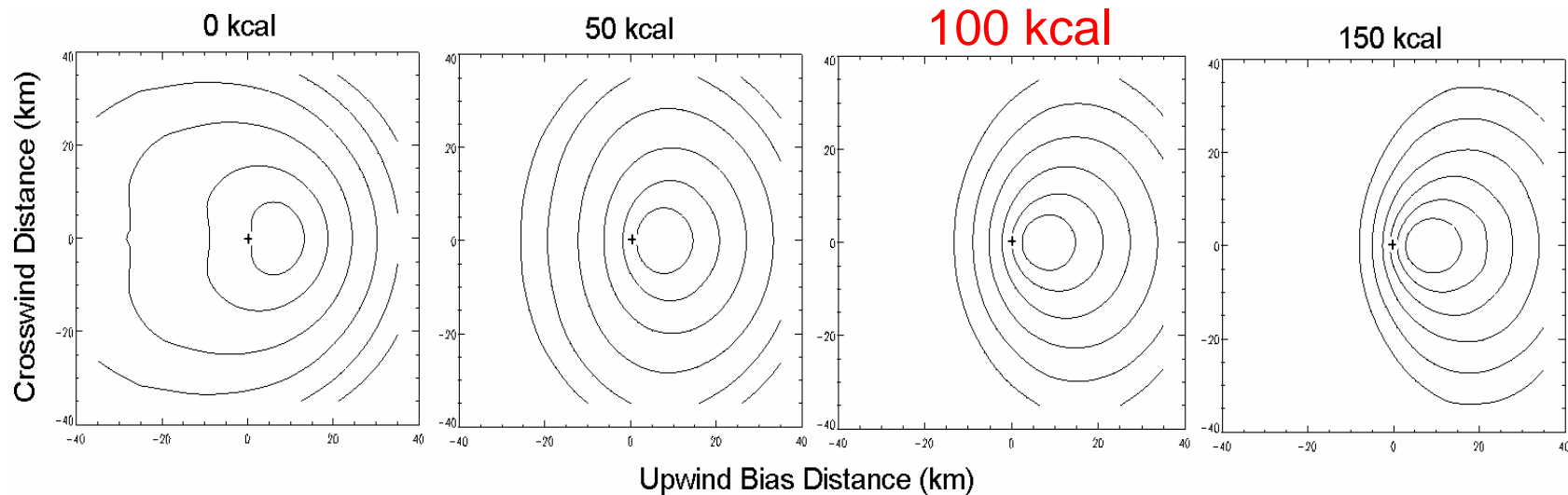
$$\sigma(E) = A_{ij} E^{-2/n}$$

(unique  $A_{ij}$  from  $A$  for each species)

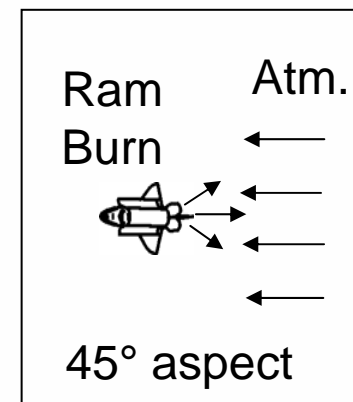
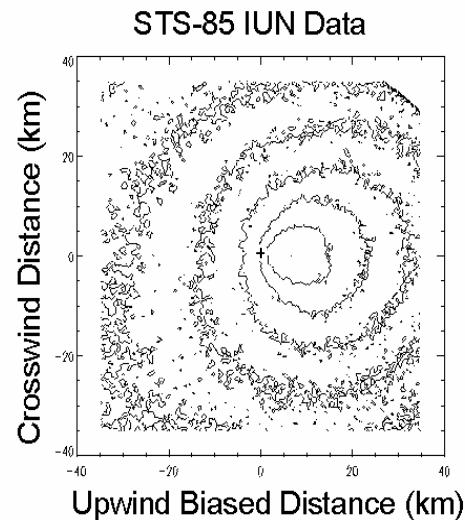
But Eq. (1) diverges from potential at hyperthermal energies.



# Sensitivity to Activation Energy

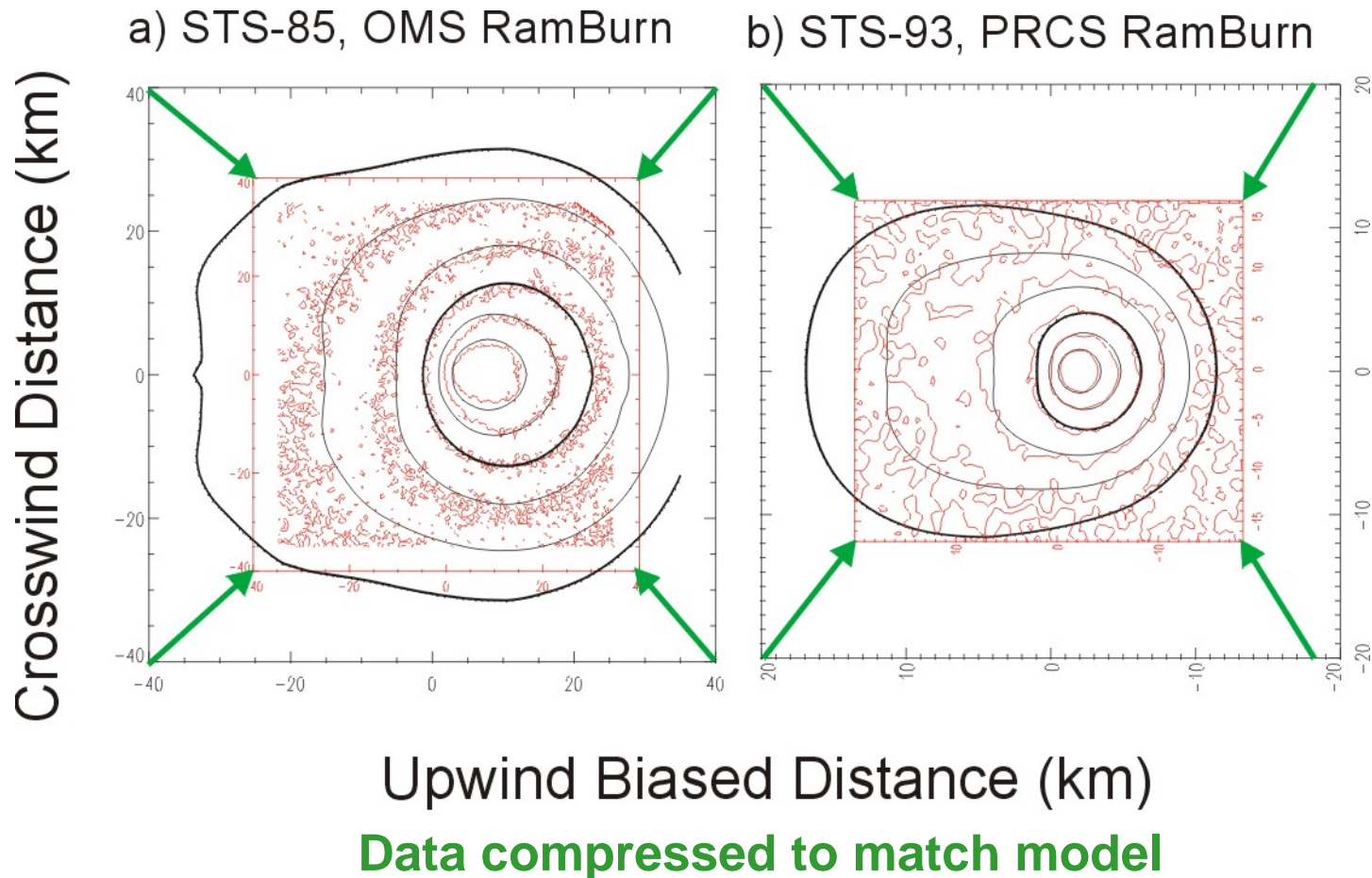


Monte Carlo analysis of UV plume as 2-step mechanism sensitive to **ACTIVATION ENERGY** in the final step.

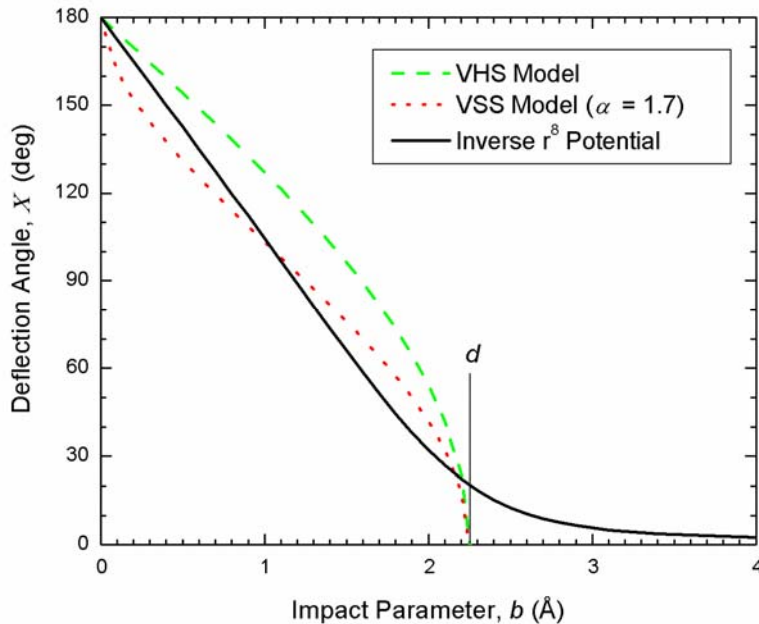


# Plume Size Mismatch

Analysis indicates mismatch between observed and modeled plume sizes for collisions at hyperthermal energies.



# Scattering Deflection Functions

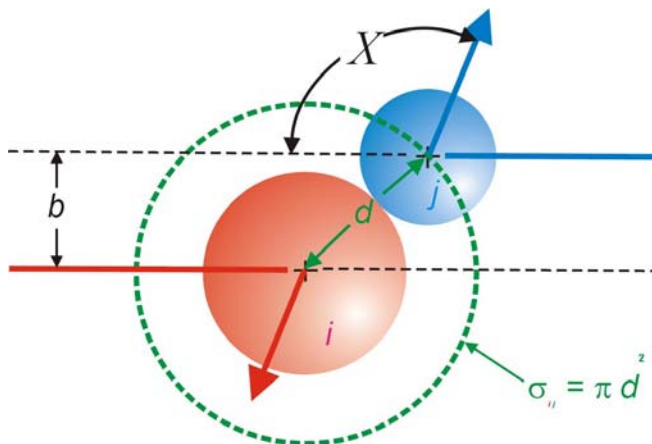


**VHS** scattering is isotropic:

$$X_{\text{VHS}} = 2 \cos^{-1}(b/d)$$

**Variable Soft Sphere (VSS)** model modifies distribution to be closer to integrated trajectory scattering from potential

$$X_{\text{VSS}} = 2 \cos^{-1}[(b/d)^{1/\alpha}]$$



# Potentials Valid at Hyperthermal Energies

# Inert Gas Diameters

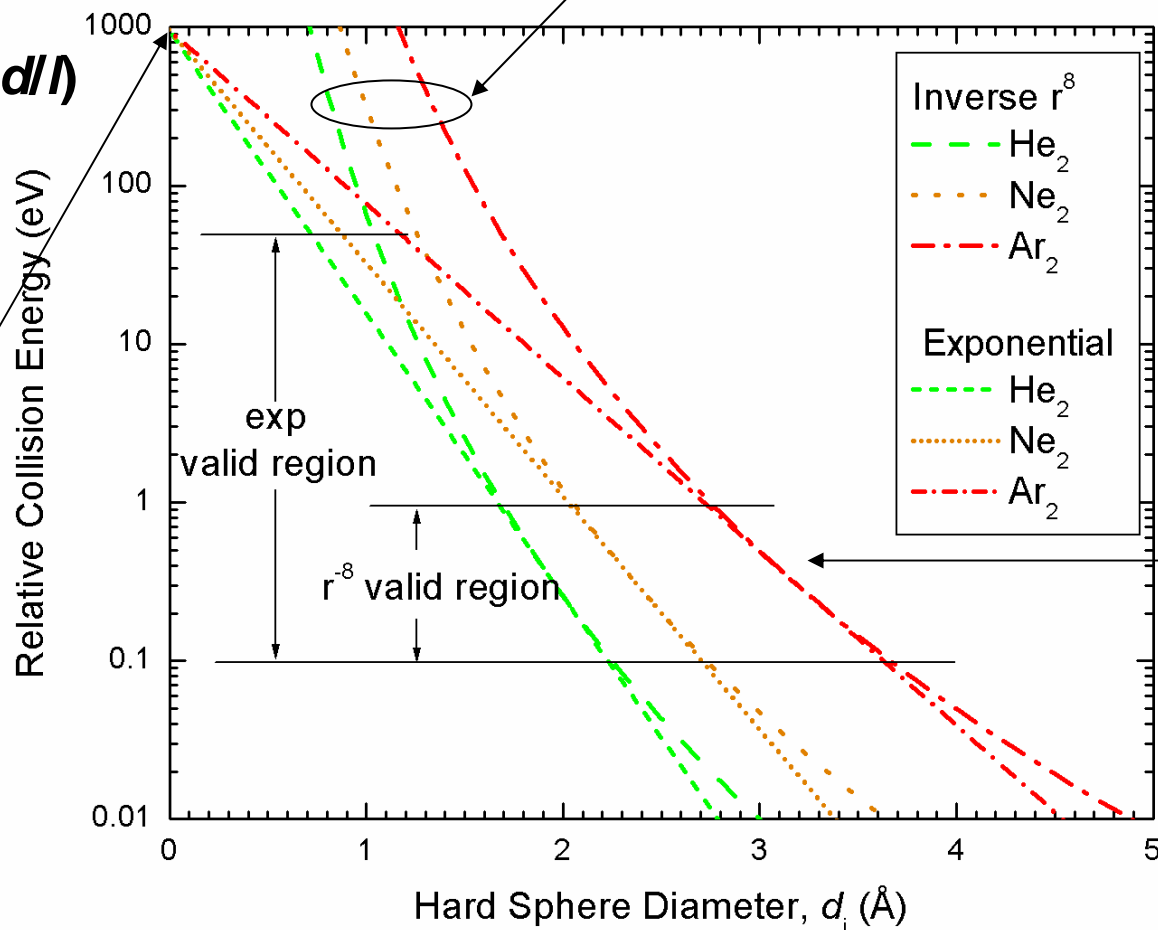
Exp fit

$$E = A' \exp(d/l)$$

found to  
have  
common  
intercept

VHS Model

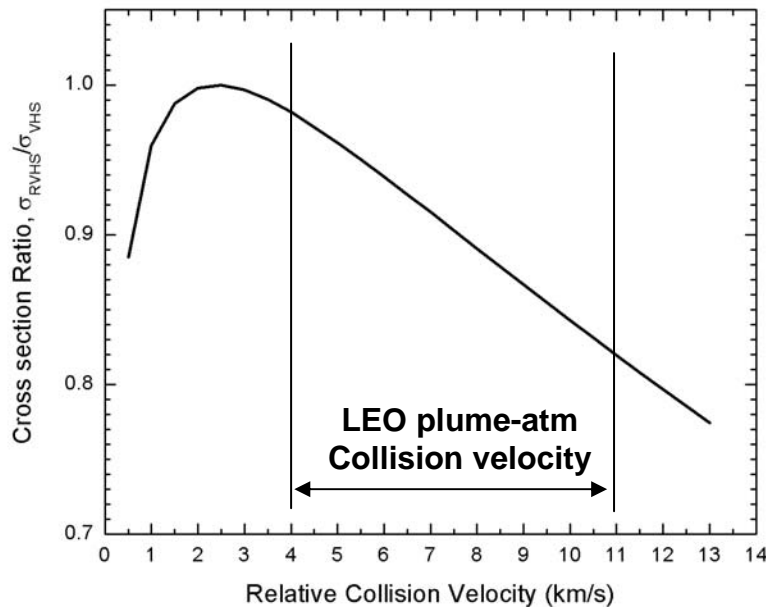
$$E = A/d^8$$



Exp fit to  
match  
slope at  
reference  
value

# Refined VHS Model (RVHS)

$\sigma_{RVHS}/\sigma_{VHS}$  ratio



## VHS Model

One parameter,  $A_{ij}$  ( $n$  constant = 8)

$$\sigma_{ij \text{ VHS}}(E) = A_{ij} E^{-2/n}$$

$$A_{ij} = [(A_{ii}^{1/2} + A_{jj}^{1/2})/2]^2$$

## RVHS Model

One parameter,  $I_{ij}$  ( $A'_{ij}$  const. = 1000)

$$I_{ij} = (A_{ij}/\pi)^{1/2} / (n E_{\text{ref}}^{1/n})$$

$$I_{ij} = (I_{ii} + I_{jj})/2$$

$$\sigma_{ij \text{ RVHS}}(E) = \pi I_{ij}^2 (\ln A'_{ij} - \ln E)^2$$

Or two parameter (more flexible):

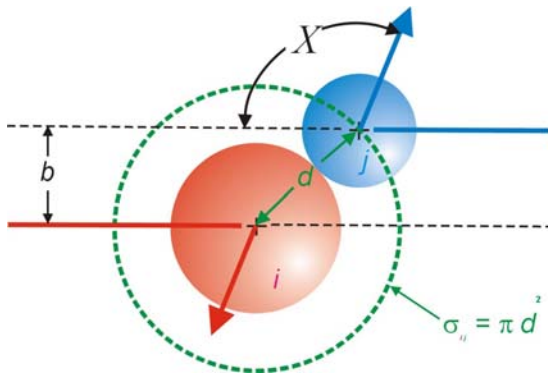
$$A'_{ij} = \exp[(I_{ii} \ln A'_{ii} + I_{jj} \ln A'_{jj}) / (I_{ii} + I_{jj})]$$

**RVHS Model valid at hyperthermal energies to ~50 eV.**

# Improved Deflection Function



# Ar-Ar Scattering Deflection at 1 eV

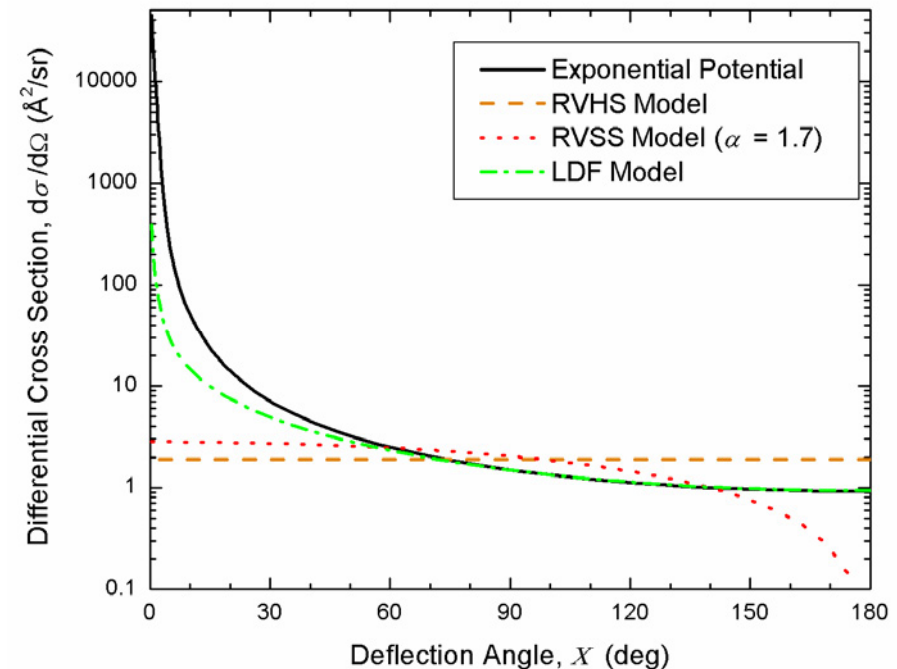
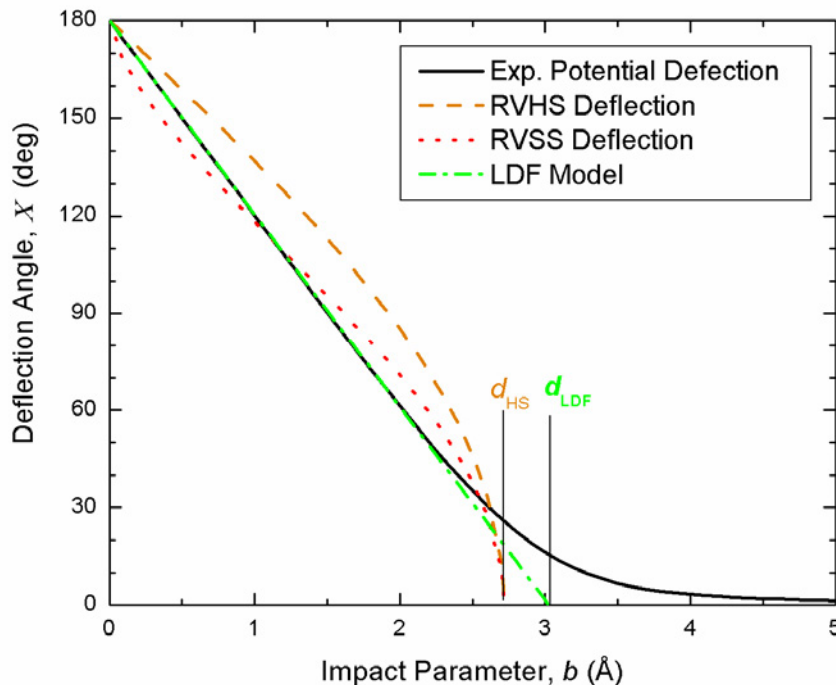


VHS isotropic scattering:

$$X_{\text{VHS}}(b) = 2 \cos^{-1}(b/d_{\text{HS}})$$

Linear Deflection Function (LDF):

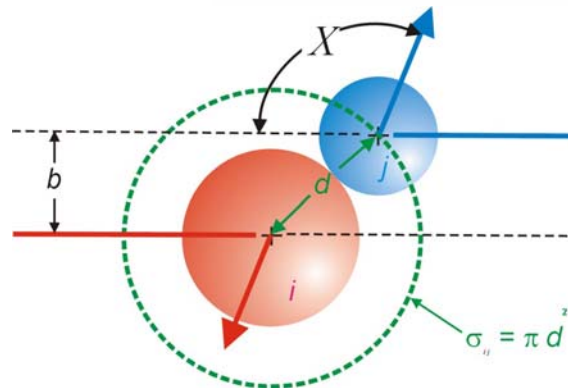
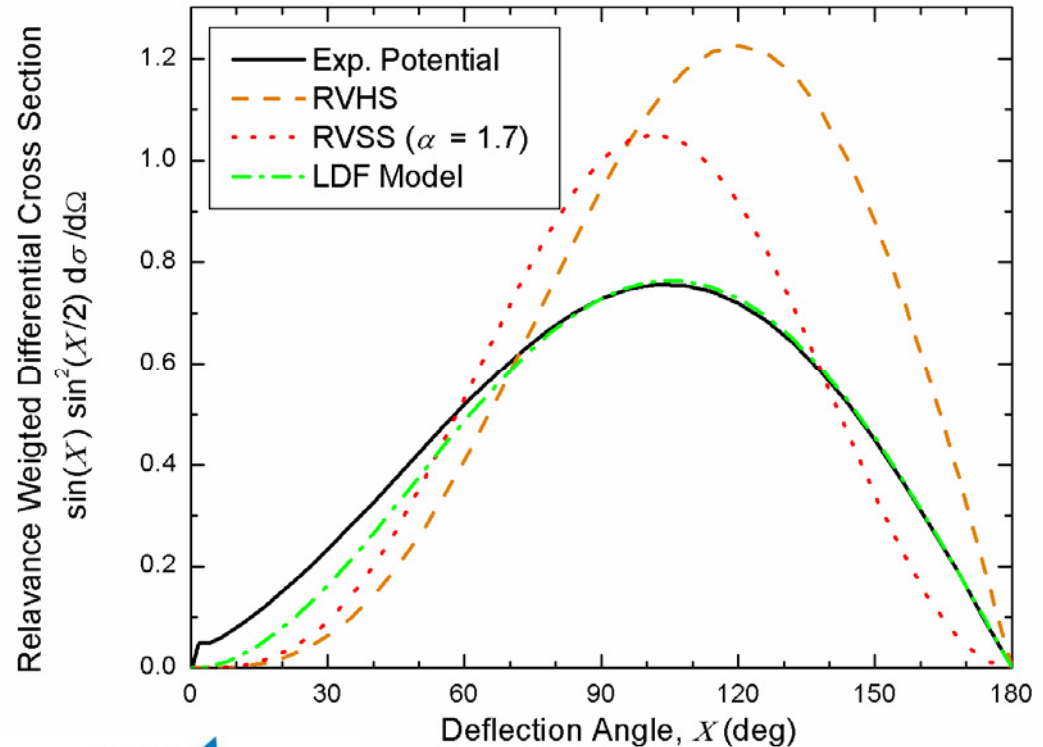
$$X_{\text{LDF}}(b) = \pi (1 - b/d_{\text{LDF}}) = \pi (1 - 0.82 b/d_{\text{HS}})$$



# Relevance Weighted Deflection

## Weighting factors

- 1)  $\sin(X)$  azimuthal dependence of accessible solid angle.
- 2)  $\sin(X/2)$  location changing dependence.
- 3)  $\sin(X/2)$  momentum transfer impacting subsequent collisions.



## Mismatched Area

**VHS = 54%**

**VSS = 30%**

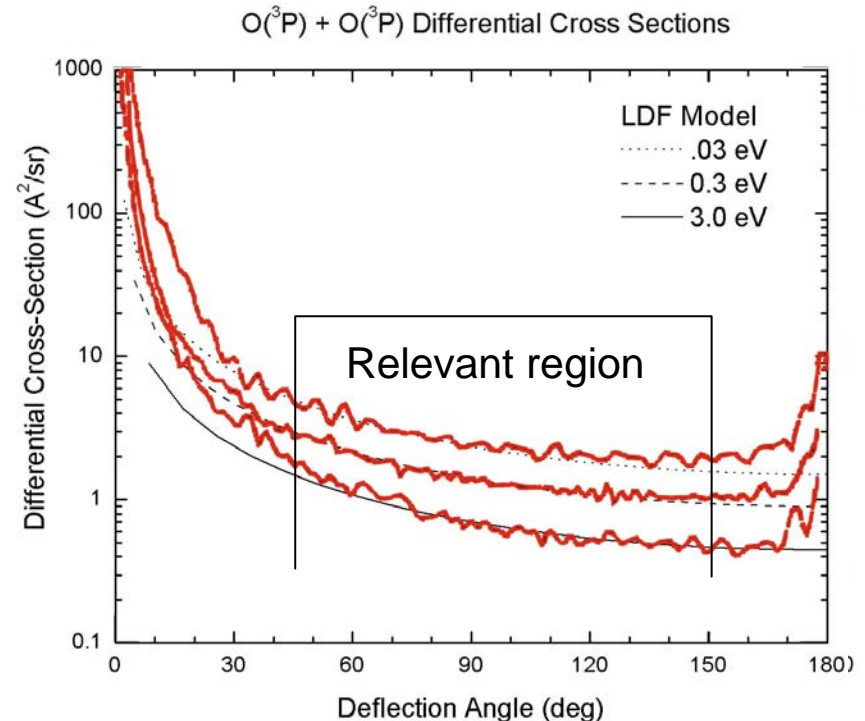
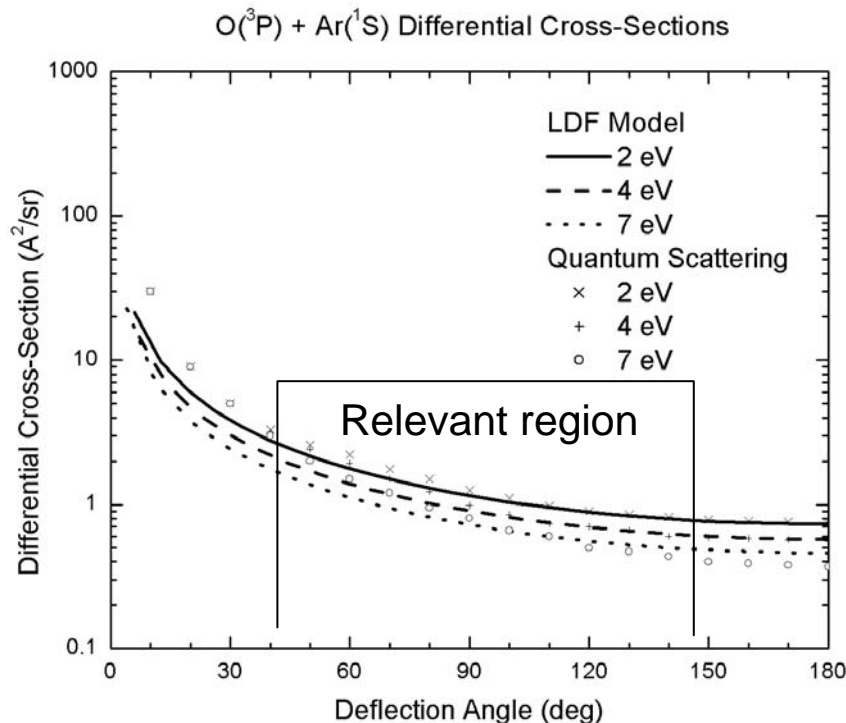
**LDF = 5%**

# Validation



# Comparison of RVHS/LDF Model to Theoretical QM Scattering

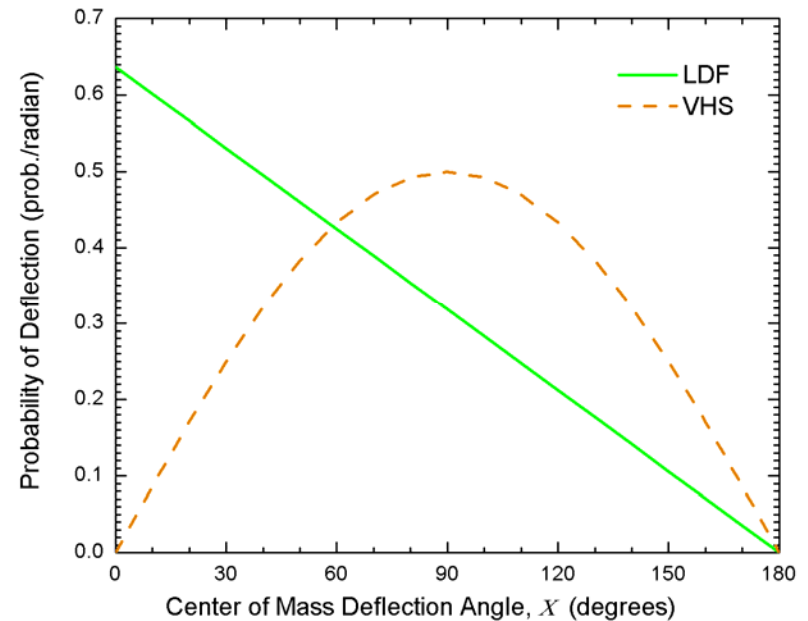
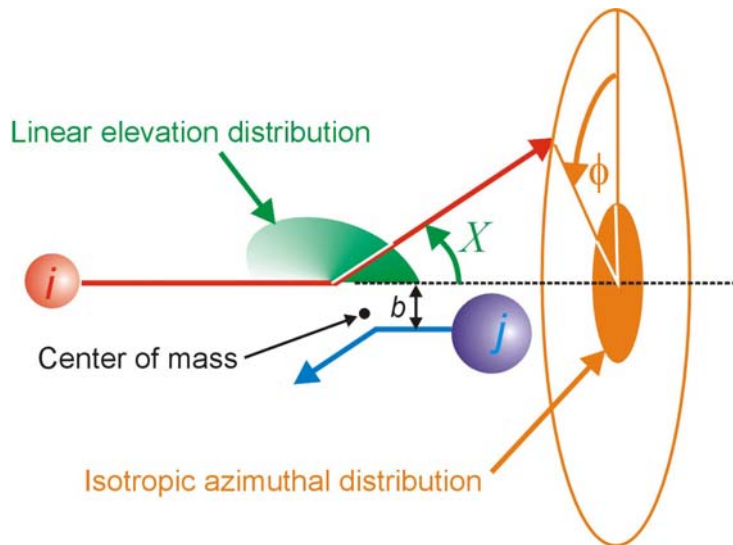
QM scattering represents statistical averages over multiple surfaces, representing approach orientations



# Implementation of Improvements



# Deflection Probability

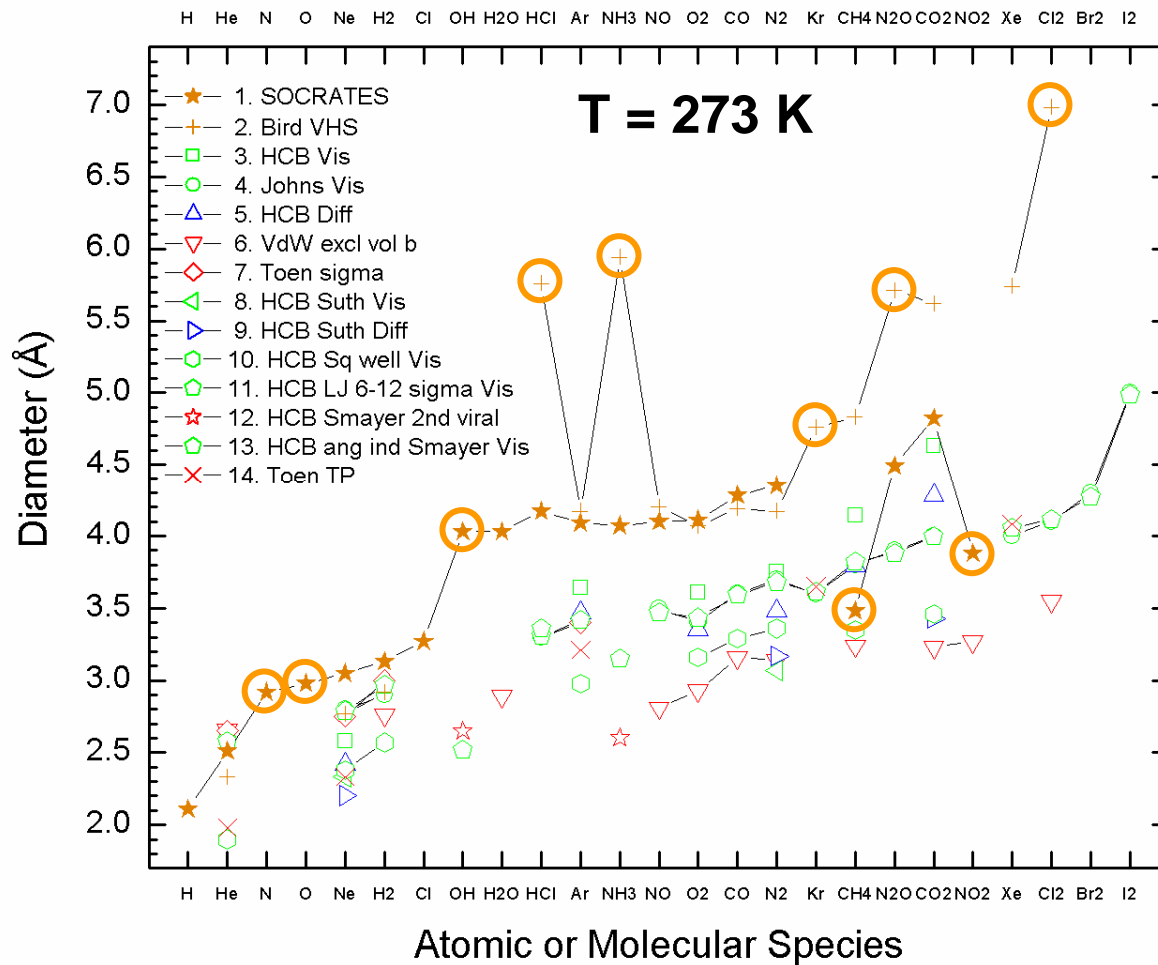


Probability of deflection described by:

$$P(X) = 2(\pi - X)/\pi^2 \quad (\text{probability per radian})$$

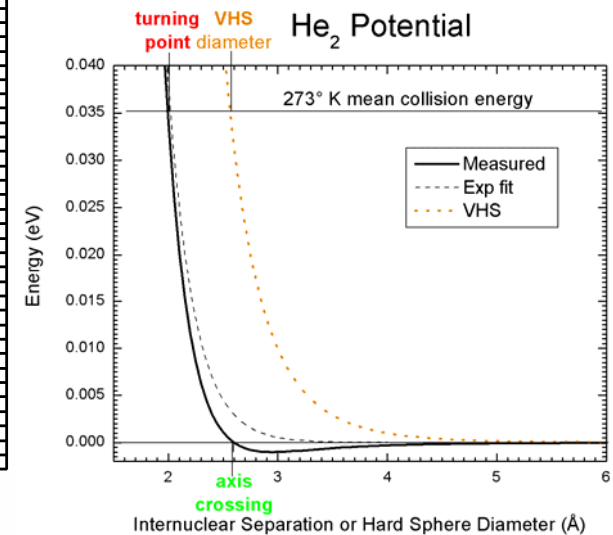
# Review of Atomic and Molecular Cross Sections

# Review of Atomic and Molecular Cross-Sections



○ = questionable

**Cross-section definitions vary**





# Summary & Conclusions

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- **Current VHS & VSS models use cross sections that are too large at hyperthermal energies.**
- **Current VHS & VSS scattering may predict erroneous plume shapes in LEO conditions.**
- **Hard sphere sizes tied to an exponential potential can extend DSMC to hyperthermal collision energies up to ~50 eV.**
- **Simple Linear Deflection Function can improve prediction of processes that may be sensitive to small numbers of collisions.**